

Feasibility study of the photonuclear reaction cross section of medical radioisotopes using a laser Compton scattering gamma source*

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In recent years, the gap between the supply and demand of medical radioisotopes has increased, necessitating new methods for producing medical radioisotopes. Photonuclear reactions based on gamma sources have unique advantages in terms of producing high specific activity and innovative medical radioisotopes. However, the lack of experimental data on reaction cross sections for photonuclear reactions of medical radioisotopes of interest has severely limited the development and production of photonuclear transmutation medical radioisotopes. In this study, the entire process of the generation, decay, and measurement of medical radioisotopes was simulated using online gamma activation and offline gamma measurements combined with a shielding gamma-ray spectrometer. Based on a quasi-monochromatic gamma beam from the Shanghai Laser Electron Gamma Source (SLEGS), the feasibility of the measurement of production cross section for surveyed medical isotopes was simulated, and specific solutions for measuring medical radioisotopes with low production cross sections were provided. The feasibility of this method for high precision measurements of the reaction cross section of medical radioisotopes was demonstrated.

Keywords: Medical radioisotope; Photonuclear reaction; GEANT4; Shanghai Laser Electron Gamma Source (SLEGS); low-background gamma-ray spectrometer

1

I. INTRODUCTION

2 In recent years, the shortage of medical radioisotopes has been repeatedly highlighted[1, 2], and the gap between the supply
3 and demand of medical radioisotopes has become increasingly prominent. Currently, the global production of medical ra-
4 dioisotopes is concentrated in a few large research reactors with a global supply strategy. These include the National Research
5 Universal Reactor in Canada, High Flux Reactor in the Netherlands, High Flux Isotope Reactor in the United States, and Mis-
6 souri University Research Reactor in the United States. However, the specific activity of the medical radioisotopes produced by
7 reactors is low, and the aging reactors built in the 1950s and the 1960s are being decommissioned. Therefore, a new methods
8 for producing medical radioisotopes with higher specific activity are urgently required[3].

9 Photonuclear reactions have attracted considerable attention worldwide because of their good selectivity, relatively single
10 reaction products, and high specific activity of the radioisotopes produced by photonuclear transmutation. The reports of
11 the Nuclear Science Advisory Committee-Isotope Subcommittee in 2009 and 2015 concluded that the study of radioisotope
12 production methods based on accelerators was essential and the photonuclear transmutation method based on an electron linear
13 accelerator was a unique source of radioisotopes [4, 5]. Recently, the Nuclear Science Advisory Committee described this
14 approach as one of the most compelling and influential opportunities for producing medical radioisotopes with high specific
15 activity.

16 Two methods for photonuclear transmutation exist. One method uses an electron accelerator to generate bremsstrahlung to
17 drive photonuclear transmutation [6]. The second method is based on photonuclear transmutation driven directly by the next
18 generation of quasi-monochromatic gamma sources [7]. However, regardless of the approach, the greatest uncertainty arises
19 from the cross section of the photonuclear reaction. For most known medical radioisotopes that can be produced, as well as
20 innovative medical radioisotopes with significant potential applications, the scarcity of data on the reaction cross section of
21 photonuclear reactions severely limits the study and development of medical radioisotopes produced by photonuclear reactions

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22 and the evaluation of photonuclear transmutation efficiency and selection of target nuclear reaction paths. In the electron-
 23 accelerator-driven scheme, the photonuclear reaction cross section determines the selection of the highest energy of the electron
 24 accelerator, which affects the maximum yield of the target isotope and specific activity of the product. Furthermore, the
 25 photonuclear reaction cross section affects the energy selection of the quasi-monochromatic gamma source and the assessment
 26 of the specific activity of the product. Therefore, measuring the photonuclear reaction cross section for medical radioisotopes
 27 of interest is highly significant.

28 High-precision measurements of the reaction cross section can be performed by offline measurements with shielding devices,
 29 which reduce interference from the surrounding environment gamma, neutron, and cosmic rays and improve the signal-to-noise
 30 ratio, even when the characteristic gamma intensity branching ratio is small. In our simulation, a quasi-monochromatic gamma
 31 beam was used to activate the target material, and the characteristic gamma rays of radioisotopes produced by photonuclear
 32 reactions were measured with an offline measuring device to detect the types and quantities of target nuclides generated in
 33 the reactive target. Finally, the reaction cross sections of photonuclear reactions (γ , n), (γ , p), and (γ , γ') were obtained. A
 34 low-background gamma-ray spectrometer was used to obtain high-precision reaction cross sectional measurements. Based on
 35 the quasi-monochromatic gamma beam of the Shanghai Laser Electron Gamma Source (SLEGS) [8, 9], the entire process of
 36 medical isotope production, decay, and measurement was simulated using the GEANT4 toolkit [10–12]. Finally, the feasibility
 37 of medical radioisotopes of interest is discussed. This study is of guiding significance for measuring reaction cross sections of
 38 medical radioisotopes produced by photonuclear reactions.

39

II. MEASUREMENT METHOD

40 The parameters for the candidate medical radioisotopes produced by the (γ ,n) and (γ ,p) reactions are listed in Table 1 [13–
 41 15]. The theoretical reaction cross section data in the energy region are obtained from the TENDL-2021 database. Most
 42 photonuclear reaction cross sections for medical radioisotopes of interest in the giant dipole resonance energy region do not
 43 have experimental data and require further accurate measurements through experiments.

44 Generally, two methods are used to measure the reaction cross section of the (γ , n), (γ , p), and (γ , γ') reactions that generate
 45 target nuclei: the first directly measures the neutron, proton, and γ' products generated by the reaction online, while the
 46 second performs offline measurements of the characteristic gamma rays of the target nucleus produced by the online activation.
 47 However, natural targets typically contain multiple isotopes, making it impossible to distinguish which isotope the neutrons,
 48 protons, and γ products detected by online measurements originated from. Furthermore, achieving 100% purity is difficult
 49 even with enriched isotopic targets, and accurate measurements of reaction cross sections with high-purity isotopic targets are
 50 expensive. The measurement of small reaction cross sections is difficult owing to the background from bremsstrahlung radiation
 51 in the gamma beam and natural background from the environment.

Table 1. Information on several medical radioisotopes in the region of interest.

Isotope	Reaction Channel	Half-life	Decay Modes	γ Energy MeV	Cross Section mb	$E_\gamma (I_\gamma)$ keV(%)
^{186}Re	$^{187}\text{Re}(\gamma, \text{n})^{186}\text{Re}$	3.72 d	$\beta^- = 92.53\%$	13.5	365.579	137.157(9.47)
^{68}Ga	$^{69}\text{Ga}(\gamma, \text{n})^{68}\text{Ga}$	67.71 m	$\varepsilon = 100.00\%$	16.5	109.096	1077.34(3.22)
^{67}Cu	$^{68}\text{Zn}(\gamma, \text{p})^{67}\text{Cu}$	61.83 h	$\beta^- = 100.00\%$	19.5	1.984	184.577(48.7)
^{47}Sc	$^{48}\text{Ti}(\gamma, \text{p})^{47}\text{Sc}$	3.35 d	$\beta^- = 100.00\%$	21	11.848	159.381(68.3)
^{64}Cu	$^{65}\text{Cu}(\gamma, \text{n})^{64}\text{Cu}$	12.701 h	$\varepsilon = 61.50\%$ $\beta^- = 38.50\%$	17	84.72	1345.77(0.47)

52 Compared to direct online measurements, offline measurements completely separate the activity measurement of radionu-
 53 clides from the photonuclear excitation process and effectively avoid interference from low-energy neutrons, X/ γ rays of various
 54 energies, and the positron pair spectrum caused by online irradiation [16–18]. Moreover, medical radioisotopes typically have
 55 long half-lives and emit gamma rays during decay, making offline decay measurements well-suited. However, most medical
 56 radioisotopes possess relatively small photonuclear reaction cross sections. Typically, the characteristic peaks of the γ spec-
 57 trum of photonuclear activation products in the irradiated target material measured offline are submerged in the environmental
 58 background. Thus, the detection limit depends on the background level.

59 Low-background gamma ray spectroscopy with germanium (Ge) detectors has become a fundamental tool for identifying and
 60 measuring the activity of radionuclides in samples, determining the emission probabilities of radioactive decay, and conducting
 61 low-level counts [19].

62 Table 2 presents a survey of reported low-background systems. All the systems possess an integrated background of \leq
 63 0.12 c/s/100cm³Ge [20–25]. Additionally, if only passive material shielding is considered, the integrated background can reach
 64 a level below 2 c/s under better conditions. Therefore, a low-background gamma-ray spectrometer for offline measurements

65 of medical radioisotopes has been proposed, which reduces the background, achieves high-precision measurements of reaction
66 cross sections, reduces the irradiation time, and saves valuable beam time.

Table 2. Survey of reported low-background γ spectrometry systems.

Active shielding	Energy range keV	Integrated background c/s/100cm ³ Ge	Reference
Plastic scintillator	100 ~ 2000	4.1×10^{-2}	Miley H S, et al.(1992)
4-sided plastic scintillator	50 ~ 3000	1.2×10^{-1}	Byun J I, et al.(2003)
6-sided plastic scintillator	100 ~ 2000	2.5×10^{-2}	Diao L J, et al. (2010)
12-sided plastic scintillator	40 ~ 2700	2.1×10^{-3}	Heusser G, et al.(2015)
9-sided plastic scintillator	40 ~ 2700	4.9×10^{-2}	Hu Q D, et al. (2016)

67 The target nuclei produced by online irradiation can be identified by their characteristic gamma energies and half-lives. N_0
68 is the number of target nuclei obtained at the end of irradiation, and N is the integral count of the gamma full-energy peak.

$$69 \quad N = N_0 I_\gamma \epsilon_\gamma C_{k\gamma} e^{-\lambda t_d} (1 - e^{-\lambda t_m}), \quad (1)$$

70 where I_γ is the gamma decay intensity obtained from the NNDC database, ϵ_γ is the detection efficiency of HPGe, which can
71 be calibrated using a gamma standard source with known intensity; $C_{k\gamma} = e^{-(\mu/\rho)\rho x}$ is the penetration factor of gamma-ray of
72 target nuclear decay; μ/ρ is the mass attenuation coefficient(cm²/g); ρx is the mass thickness of the target(g/cm²); λ is the
73 decay constant of the target nucleus; t_d is the time interval between the end of irradiation and the start of measurement; and t_m
74 is the time of offline measurement. As a general activation measurement [26],

$$75 \quad N_0 = \sigma(E) N_t Q C_{kbeam} \int_0^{t_i} \varphi(t) e^{-\lambda t} dt, \quad (2)$$

76 where $\sigma(E)$ is the energy dependent reaction cross section; N_t is the surface density of the target nucleus (atoms/cm²); Q
77 is the abundance of the target isotope in the target; C_{kbeam} is the penetration factor of the incident gamma beam in the target;
78 $\varphi(t)$ is the γ beam intensity as a function of time; and t_i is the irradiation duration. If $\varphi(t)$ is approximated as a constant, then

$$79 \quad N_0 = \frac{\sigma(E) \phi N_t Q C_{kbeam} (1 - e^{-\lambda t_i})}{\lambda}, \quad (3)$$

80 where ϕ is the integrated gamma-ray flux; Because N_0 can be measured from N using Eq. (1), the reaction cross section
81 can be obtained from Eq. (2). The gamma flux from the real measurement of SLEGS was found to be stable because of the
82 stable electron beam intensity of the SSRF storage ring and the laser beam used for Compton scattering. A specific form
83 of the beam intensity $\varphi(t)$ was required to perform the simulation. A constant beam-intensity approximation was used to
84 study the feasibility of cross-sectional measurements based on realistic beam-intensity measurements. After determining the
85 measurement method for the photonuclear reaction cross section, a low-background gamma spectrometer was constructed
86 using GEANT4 and the feasibility of the method was assessed by simulating the entire process of photonuclear reactions for
87 producing medical radioisotopes and offline measurements.

88 III. SIMULATION MODELING

89 GEANT4 is a Monte Carlo simulation toolkit, which is widely used in particle physics, astrophysics, nuclear physics, medical
90 physics, radiation protection, and other fields [12]. GEANT4 enables accurate numerical simulations of interactions between
91 matter and particles, including particle transport, energy deposition, electromagnetic interactions, and nuclear reactions. It
92 also supports extensions in various aspects, such as particle type, geometry, material properties, detector type, and computer
93 operating systems. The main advantages of GEANT4 are its high reproducibility and reliability. Based on GEANT4, we
94 developed a program for simulating medical isotope production, decay, and measurement and performed full-scale simulations.

95 A. Medical isotope production

96 A Laser Compton Scattering (LCS) light source is a new X-ray or Gamma-ray source based on the interaction of a relativistic
97 electron beam with laser photons. It is characterized by high energy, short wavelength, fast pulses, and high peak brightness,

98 and has become an important option for advanced international light source technology [27]. SLEGS) produces gamma rays
 99 in the energy range of 0.4–20 MeV, thereby covering the energy range from the nuclear structure to giant resonance (keV to
 100 MeV) in nuclear physics research. The gamma ray flux integrated over the entire spectrum can reach 10^5 - 10^7 phs/s and is
 101 continuously adjustable. Collimation technology can be used to achieve an energy spread greater than 5% [8, 28]. Therefore,
 102 in our simulation, we used a gamma beam with an intensity and energy spread of 10^7 phs/s and of 5%, respectively, to activate
 103 the Ti target and produce the target medical isotope, ^{47}Sc , via the $^{48}\text{Ti}(\gamma, \text{p})^{47}\text{Sc}$ reaction for further analysis.

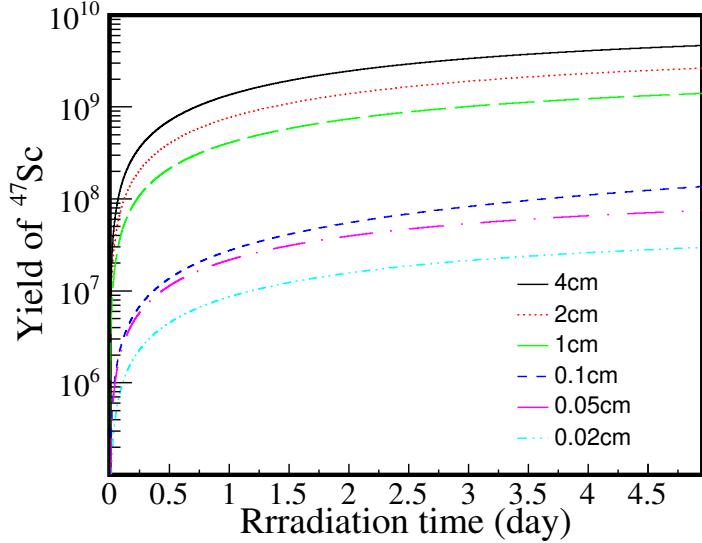


Fig. 1. Variation of the yield of ^{47}Sc with irradiation time for targets of different thicknesses.

104 Fig. 1 shows that within the first half day of irradiation, the yield of ^{47}Sc increases rapidly, and after the irradiation time
 105 exceeds half a day, the yield gradually approaches a saturation value of one. The choice of the target thickness was related to
 106 the penetration factor of the incident gamma beam in the target(C_{kbeam}). As the thickness of the target increased, the photons
 107 needed to penetrate a longer distance through the target material, resulting in a decreased photon count. Simultaneously,
 108 multiple scattering inside the target produced a broader distribution of photon energies. In addition, the choice of the target
 109 thickness was also related to the penetration factor of the gamma rays produced by the target nucleus decay ($C_{k\gamma}$). The gamma
 110 rays produced by the decay of the target nucleus attenuated with increasing thickness of the target, and the integral count of the
 111 gamma full-energy peak decreased, which affected the measurement.

112

B. Low-background gamma-ray spectrometer

113 The significant effect of the background radiation on the measured energy spectrum results in unreliable analytical results.
 114 Background radiation primarily originates from three sources: natural environmental radiation from the laboratory environment,
 115 radioactive background from the detection components and shielding materials, and cosmic ray contributions. Low-background
 116 gamma spectrometers must be shielded against background radiation to achieve high-precision reaction cross section measure-
 117 ments of medical radioisotopes.

118 Many low-background gamma-ray spectrometers have been constructed domestically and internationally. Moreover, coun-
 119 tries such as China, France, the United States, and Japan have established underground laboratories at different depths to
 120 facilitate research in low-background measurement fields. Representative devices abroad include those of the same type estab-
 121 lished by Miley at the Pacific Naval Laboratory in 1991 [20], Byun at the Korea Atomic Energy Research Institute in 2001 [21],
 122 Semkow et al. in the United States in 2002 [19], and Heusser et al. in Germany [23, 24]. Such devices have also been built
 123 in laboratories in China, including the China Institute of Atomic Energy [22], Institute of High Energy Physics of the Chinese
 124 Academy of Sciences, and Third Institute of Oceanography of the State Oceanic Administration [25].

125 Based on existing low-background gamma spectrometers, a low-background gamma spectrometer was designed using
 126 GEANT4 simulations to achieve a shielding effect. The shielding structure is illustrated in Fig. 2 [29].

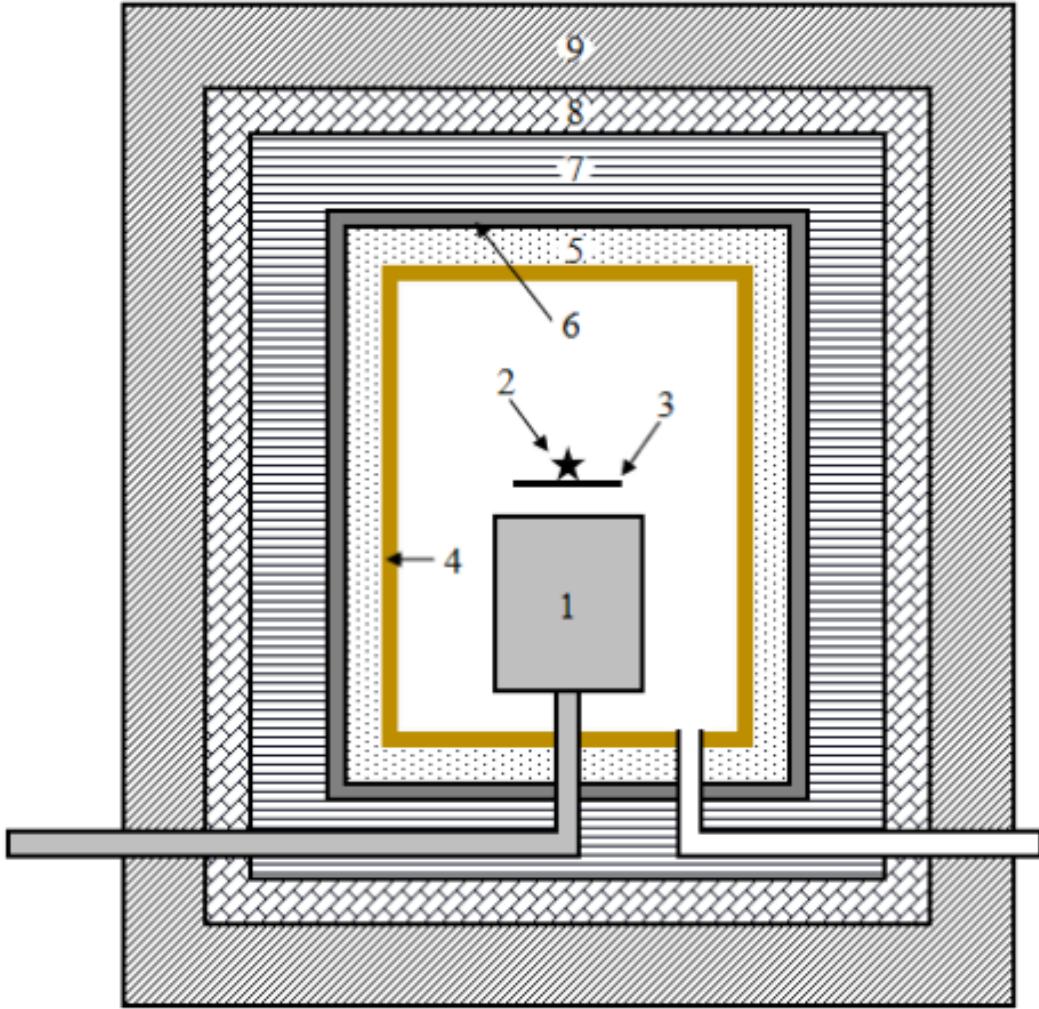


Fig. 2. Low-background gamma-ray spectroscopy with shielding structure: 1.HPGe detector, 2.sample to be measured, 3.plastic holder, 4.the copper liner(2 mm-thick), 5.inner lead(50 mm-thick), 6. cadmium absorber(3 mm-thick), 7.borated polyethylene(100 mm-thick), 8.plastic scintillator(50 mm-thick), 9.outer lead(100 mm-thick).

Using a high-purity germanium detector for a low-background gamma spectrometer requires careful consideration of shielding from various backgrounds. The gamma ray intensity decreases drastically as the atomic number of the material increases because materials with higher atomic numbers possess larger gamma attenuation factors than those with lower atomic numbers [30, 31]. Common high-Z materials include lead, oxygen-free copper, and steel; however, iron is easily contaminated with ^{60}Co during smelting, and copper has a large thermal neutron capture reaction cross section. Considering factors such as the price, atomic number, and mechanical properties, lead is the best choice for gamma shielding materials.

Cosmic rays in the environment produce secondary particles, such as photons, neutrons, and electrons, when they undergo muon capture in materials with large atomic numbers, such as lead [32–36]. Therefore, the second layer of the shielding device considers neutron shielding. Neutrons must undergo deceleration and absorption. Water, paraffin, and polyethylene are widely used as slowing down materials [37]. Plastic scintillators or polyethylene can be used as a second layer to slow down fast neutrons.

The third layer is used to absorb thermal neutrons. ^{10}B is an excellent absorber of thermal neutrons and B_4C has a B/C ratio of 0.7828, resulting in a very large neutron capture reaction cross section. Thus, it can effectively absorb decelerated neutrons. Additionally, cadmium has a large absorption reaction cross section for thermal neutrons. Therefore, boron-containing polyethylene can be used to slow down and absorb neutrons, whereas cadmium can be used to absorb thermal neutrons [38]. However, cadmium atoms emit gamma rays with an energy of 2.3 MeV after capturing neutrons. Therefore, a low-background lead must shield this portion of the gamma rays.

144 Finally, other low-Z materials, such as organic glass or copper, can be added to the inner lining to shield against impurities,
 145 such as ^{210}Pb , its daughter nucleus ^{210}Bi in lead, and the characteristic X-rays of lead [39]. The shielding structure was deter-
 146 mined through simulations to select appropriate shielding materials and optimize their thicknesses. The final shield structure
 147 from the outside to the inside was determined to be: 100 mm thick lead, 50 mm thick plastic scintillation, 100 mm thick borated
 148 polyethylene, 3 mm thick cadmium, 50 mm thick lead, and 2 mm thick oxygen-free copper, which was consistent with the
 149 low-background gamma spectrometer designed by Hu et al. [25].

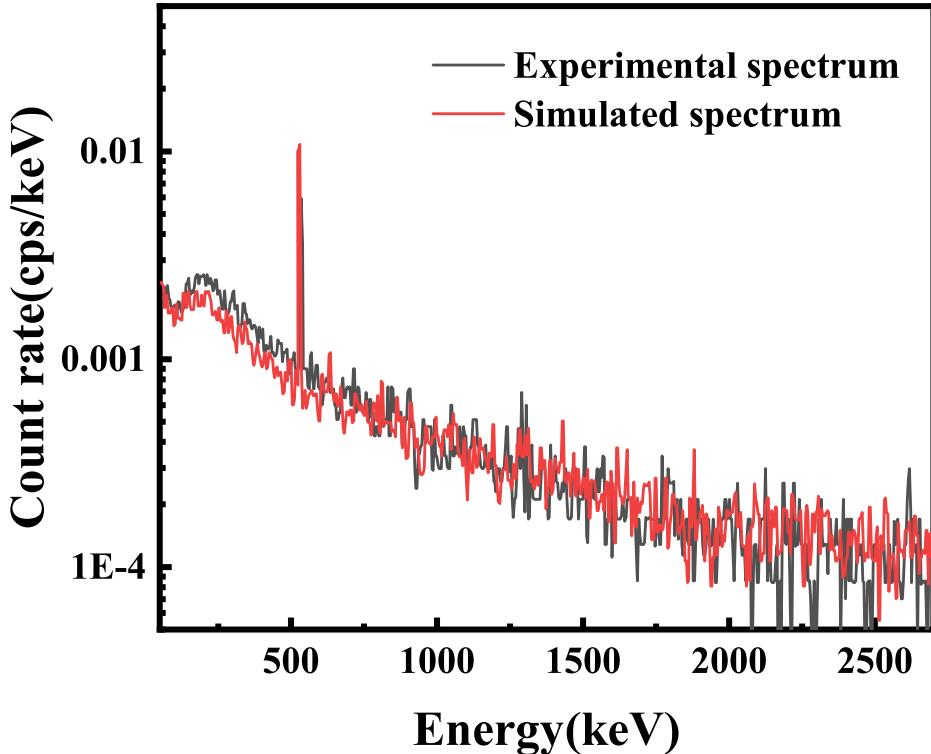


Fig. 3. Comparison between the simulated and experimental spectra.

150 In Fig. 3, a comparison of the simulated HPGe energy deposition spectrum with the results obtained by Hu et al., reveals a
 151 similar trend, and the count rate of the 511 keV peak in the spectrum possesses the same order of magnitude (approximately
 152 8×10^{-3} cps). It is essential to note that because of the shielding configuration employed, specifically the incorporation of
 153 an inner lead layer in our shielding system, the 478 keV peak is obscured and consequently, not evident in Fig. 3. In the
 154 low-energy range, the count rate of the experimental spectrum exceeds that of the simulated spectrum owing to the differences
 155 in the background and radioactivity of the shielding material and detector. Thus, the reliability of the simulations was verified.

156

C. Medical isotope decay and measurement

157 Based on the passive-shielding conditions shown in Fig. 2, the total integral background count rate in the energy range
 158 of 100~2700 keV obtained by the simulation is 0.22 c/s/100cm³Ge, whereas under the better condition of using only lead
 159 shielding, the total integral background count rate in the energy range of 100~2700 keV may reach 1 cps [25, 40, 41]. To
 160 reduce simulation complexity, we used lead shielding only in the following simulation. Based on the spectrometer constructed
 161 in the GEANT4 simulation program, the number of target nuclei ^{47}Sc produced was considered as the input for offline decay
 162 measurement simulation when the offline measurements lasted for only 1 h and only lead shielding was used.

163 In Fig. 4, we present the spectra obtained by simulations under different conditions (Shanghai electron laser gamma source
 164 laboratory environment background, low background shielding device, and neglecting the environmental background). After
 165 background subtraction, the integral count rate of the gamma full-energy peak from the decay of ^{47}Sc is 0.16 c/s at $E_{\gamma}=$
 166 159 keV. When measured in the environmental background, the gamma full-energy peak of ^{47}Sc is completely submerged in
 167 the background. Low-background shielding effectively reduced the lower limit of detection was, and the integral count of the
 168 gamma full-energy peak of the characteristic peak was identifiable.

169 Therefore, the cross sections for medical radioisotopes produced by photonuclear reactions were efficiently measured by

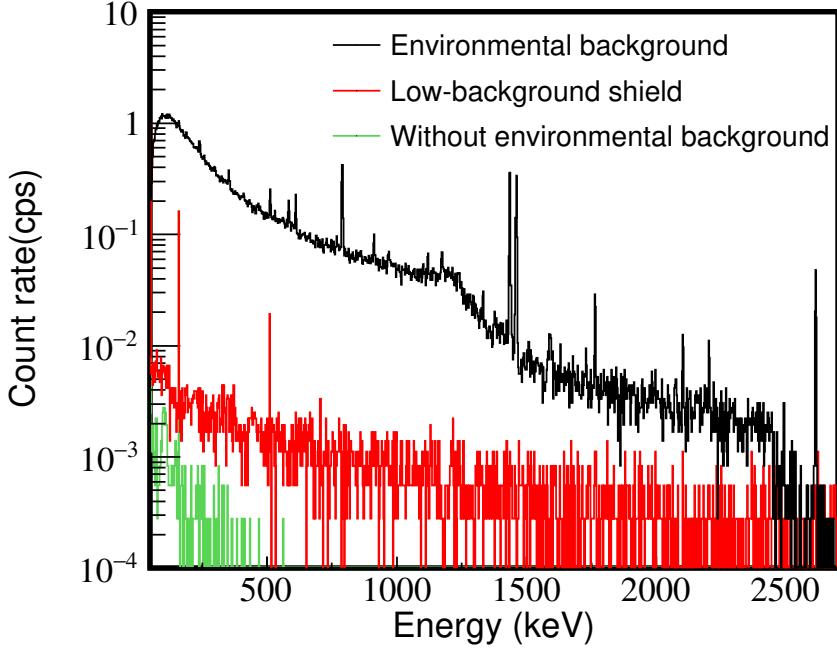


Fig. 4. Simulated spectra of ^{47}Sc under different conditions.

170 reducing the background. In addition, factors such as the irradiation time, measurement time, and beam intensity affected cross
 171 section measurements. In the next section, we discuss the detection lower limit through computational simulations.

172

IV. FEASIBILITY OF MEASUREMENT

173 Our simulation program includes five control parameters: irradiation time, measurement time, time interval between the end
 174 of the irradiation and the beginning of the measurement, thickness of the target, and beam intensity. Considering the influence
 175 of the background in a real environment, the background was considered as the sixth control parameter. Based on SLEGS, the
 176 gamma beam intensity factor can be set to 10^7 phs/s [8].

177 First, we considered the background factor. According to Eq. (1), N is the integral count of the gamma full-energy peak
 178 when the background is neglected. However, the detector measures the integral count of the gamma full-energy peak produced
 179 by the decay of the target nucleus in combination with the background. Therefore, we obtained the following relationship:

180

$$N = C - C_0, \quad (4)$$

181 where C and C_0 denote the integral count of the gamma full-energy peak produced by the decay of the target nucleus measured
 182 by the detector and the background count by the low-background detection system (considering only lead shielding), respec-
 183 tively. For realistic measurements, the relative statistical error of the counts was set to 10%. According to the error propagation
 184 formula, the relative statistical error is expressed by Eq. (5)

185

$$v = \frac{\sqrt{C + C_0}}{C - C_0}. \quad (5)$$

186 Subsequently, the target thickness was considered. According to Eqs. (1) and (2), the thickness of the target mainly affects
 187 the attenuation coefficient and area density. We constructed a function $f(x)$ that varies with the thickness of the target, as shown
 188 in Eq. (6) as follows:

$$\begin{aligned}
189 \quad f(x) &= N_t C_{k\gamma} C_{kbeam} \\
&= \frac{N_A \rho x e^{-(\mu/\rho)\rho x} e^{-(\mu'/\rho)\rho x}}{M}, \quad (6)
\end{aligned}$$

190 where $N_t = \frac{N_A \rho x}{M}$, N_A is the Avogadro constant; M is the molar mass; ρx is the mass thickness of the target; μ is the
191 attenuation coefficient of the photon beam incident on the target during online activation; and μ' is the attenuation coefficient
192 of de-excitation gamma escaping the target in offline measurements. Using $^{69}\text{Ga}(\gamma, n)^{68}\text{Ga}$ as an example, the relationship
193 between $f(x)$ and x is as shown in Fig. 5.

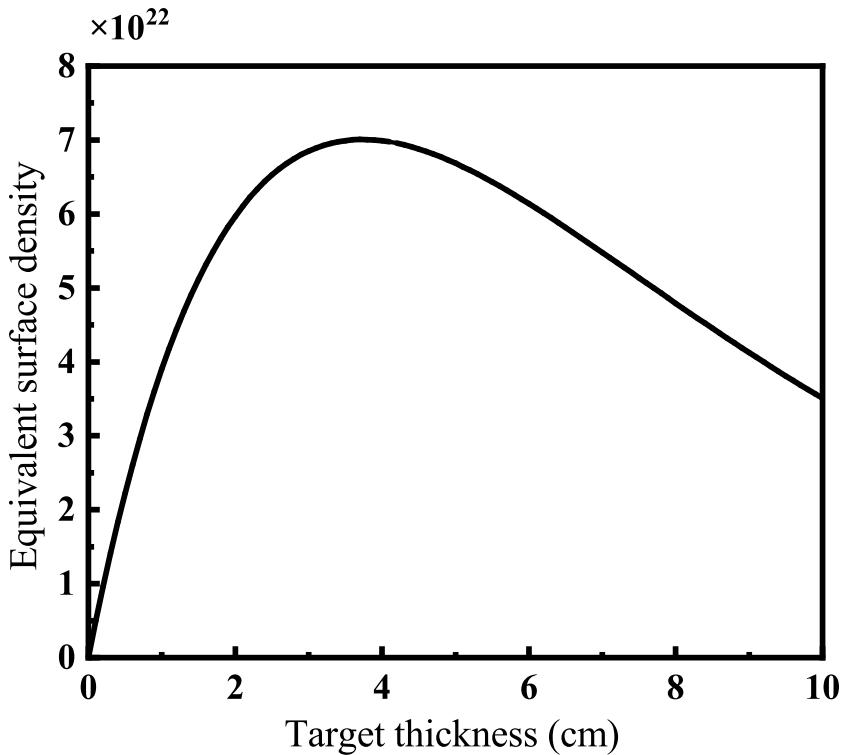


Fig. 5. Dependence of the equivalent surface density on the target thickness for $^{69}\text{Ga}(\gamma, n)^{68}\text{Ga}$

194 According to Fig. 5, the function $f(x)$ has a maximum value. Rewriting Eqs. (1) and (2) as functions of $f(x)$, as shown in
195 Eq. (7), we obtain:

$$196 \quad N = \frac{\sigma(E) \phi Q I_\gamma \epsilon_\gamma e^{-\lambda t_d} (1 - e^{-\lambda t_m}) (1 - e^{-\lambda t_i}) f(x)}{\lambda}, \quad (7)$$

197 where $f(x)$ is proportional to N . The maximum integral count N can be determined using $f(x)$ when the other conditions
198 are fixed. In realistic measurements, the thickness of the target nucleus affects the count rate of the characteristic gamma
199 owing to the inevitable attenuation of the gamma incident on the target nucleus and the self-absorption of the target nucleus
200 during deexcitation. Therefore, the thickness must be determined based on practical considerations among other factors. For
201 thicknesses ranging from zero to the optimal value, $f(x)$ increased monotonically with x . Based on this property, the detection
202 limit can be determined by combining time factors.

203 The time factors include the irradiation time t_i , measurement time t_m , and time interval from the end of irradiation to the
204 beginning of measurement t_d . Here, t_d was uniformly set to 5 min, and the relationship between t_i and t_m was determined
205 from Eq. (7). In other words, when the other conditions were fixed, one quantity increased whereas the other decreased. One
206 can define $A = t_i t_m$. Considering the decay of the target nucleus, t_m is limited to 900-3600 s, and t_i was limited to within 24 h
207 in a realistic case.

208 Three limiting factors: x , t_m , and t_i were considered. When x had a minimum value of 0.01 cm, offline measurements were
 209 used to measure the cross section of medical radioisotopes generated by photonuclear reactions with a 0.01 cm thick target if
 210 the simulated values of t_m and t_i were within their respective limits (i.e., t_m was between 900-3600 s and t_i was within 24
 211 h). Measurements were easier for smaller values of A because less time was required for irradiation and measurement. If t_m
 212 and t_i were outside their respective limits when x was set to 0.01 cm, the measurement of medical radioisotopes generated
 213 by photonuclear reactions was not feasible at this thickness. The detection limit was determined by gradually increasing the
 214 thickness in steps of 0.01 cm, and the difficulty in detection was indicated by the values of x and A .

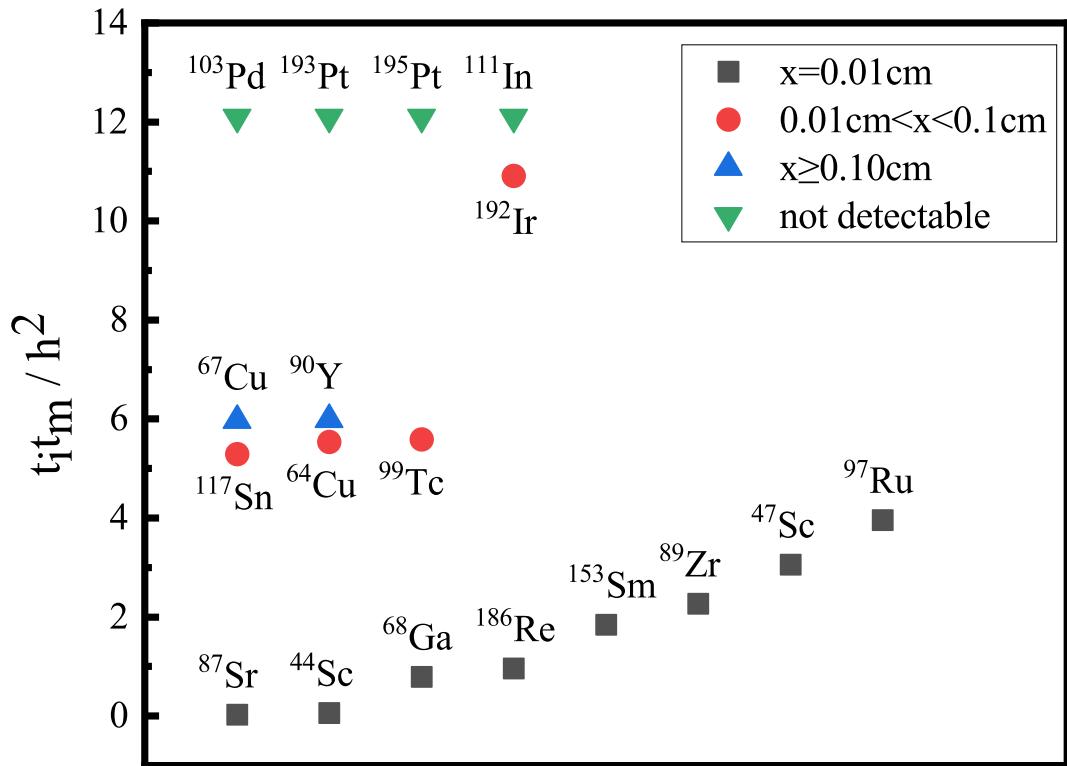


Fig. 6. Feasibility of reaction cross section measurement for some medical radioisotopes, where t_m , t_i , and h represent the time of offline measurement, irradiation duration, and unit of time in hour, respectively.

215 Some medical radioisotopes of interest were selected, and the simulation was performed using the aforementioned method;
 216 the results are shown in Fig. 6. When $x = 0.01$ cm, ^{87}Sr , ^{44}Sc , ^{68}Ga , ^{186}Re , ^{153}Sm , ^{89}Zr , ^{47}Sc , and ^{97}Ru can be used to measure
 217 the production reaction cross section. Smaller values of A indicate shorter irradiation and measurement times. However, ^{45}Ti ,
 218 ^{103}Pd , ^{193}Pt , ^{195}Pt , and ^{111}In could not be measured within an irradiation time of 24 h and a detection time of 3600 s, even with
 219 the optimal thickness.

220 Several methods can be used to enhance the measurement of reaction cross sections for these medical radioisotopes, such
 221 as transferring to stack targets, switching to enriched isotopic targets, increasing the intensity of the gamma beam, and using
 222 low-background gamma spectrometers with better shielding.

223 The characteristic gamma decay can be reduced by stacking several targets together to form a stacked target. Compared to
 224 other methods, its implementation is easy. Taking $^{112}\text{Sn}(\gamma, p)^{111}\text{In}$ as an example, natural and stack targets were used for the
 225 simulation. The thicknesses of the natural and stack targets were assigned the same value (1 mm) to allow easy comparison of
 226 the results. Thus, the natural target was 1 mm thick, and the stack target was divided into five pieces, each with a thickness of
 227 0.2 mm. The results of the comparison are presented in Fig. 7.

228 For the characteristic gamma $E_\gamma = 171.29$ keV, the count rate of the full-energy peak measured using the natural targets
 229 was 0.027 c/s whereas the count rate measured using the stack targets was significantly higher than that of the natural targets at
 230 0.039 c/s. However, the low abundance of ^{112}Sn in the Sn target resulted in a low yield of ^{111}In . During the actual measurement,
 231 the existence of the background resulted in relative error ν exceeding 10%, even with the use of a stack target. Therefore, for
 232 cross section measurements of $^{112}\text{Sn}(\gamma, p)^{111}\text{In}$, enriched isotopic targets can be used to improve feasibility. With 100% isotopic
 233 targets, the count rate at $E_\gamma = 171.29$ keV can be increased to 2.409 c/s, and the characteristic gamma full-energy peak can be
 234 detected under a low background shield, as shown in Fig. 8.

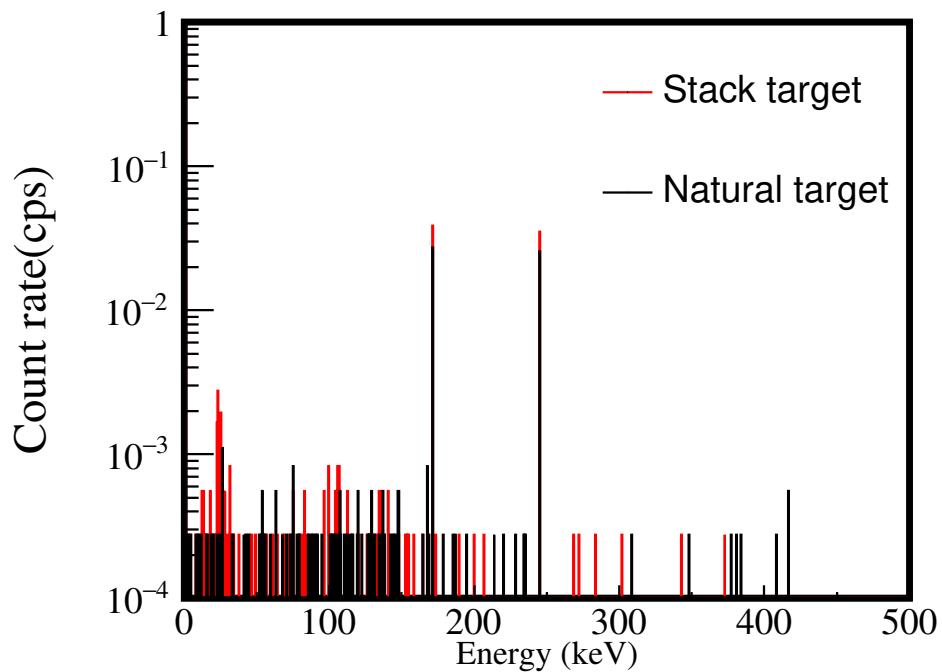


Fig. 7. Comparison of the count rates of the natural and stack targets($^{112}\text{Sn}(\gamma,\text{p})^{111}\text{In}$).

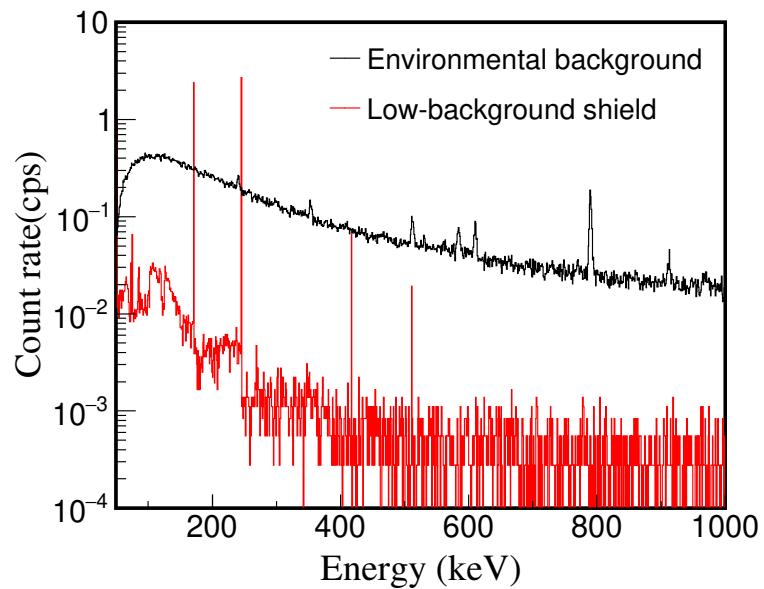


Fig. 8. Decay spectra of ^{111}In under environmental background and low background shield with enriched isotope target.

235

V. CONCLUSION

236 Available data on gamma transmutation cross sections for medical radioisotopes are scarce. Measurements of photonuclear
 237 reaction cross sections are useful for filling the gaps in data from gamma transmutation experiments, reducing large data er-
 238 rors, and resolving divergences between various theoretical calculations and data. In this study, the generation, decay, and
 239 measurement of medical radioisotopes were simulated using GEANT4 combined with a shielding gamma-ray spectrometer.
 240 Low background shielding can improve the signal-to-noise ratio, facilitate high-precision measurements, and save the valuable
 241 beam time. Based on SLEGS, the feasibility of specific medical radioisotope reaction cross section measurements was pre-
 242 sented. SLEGS, the only available gamma facility in China capable of providing intermediate-and high-energy, high-intensity,
 243 quasi-monochromatic, energy continuously adjustable gamma beam, is expected to provide an important platform for studying
 244 photonuclear reaction cross sections for medical radioisotopes of interest.

245

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 247 driven by γ -ray beam transmutation.

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